

Distribution Pattern of the Duplication of Discoveries

PRICE¹ conjectured that a Poisson distribution might be a good fit for the pattern of incidence of multiple discoveries. We have fitted a modified Poisson distribution to the frequency of duplication of discovery of antibiotics.

We have considered the discovery of an antibiotic to have been duplication if it was identified with another antibiotic and so reported in published documents irrespective of whether the compounds were produced one and the same or different species of microorganisms. We used the data reported earlier¹ on the frequency of duplication of discovery of antibiotics during 1907-19, after correcting a few minor discrepancies. As there is practically no duplication of discovery of antibiotics for bacteria, we have dealt only with the pattern relating to two groups: (1) fungi, algae and lichens, and (2) actinomycetales.

A normal Poisson distribution did not fit the distribution pattern of duplications, but a modified version² did. For such a distribution, the p.d.f. is

$$\left(\frac{c}{c+1}\right)^p \left\{ \frac{p(p+1)(p+2) \dots (p+r-1)}{(r-1)!(r+1)^r} \right\} \quad (1)$$

where p and c are constants to be estimated using the following relations

$$\text{mean of } X = p/c \quad (2)$$

$$\text{var}(X) = p/c + p/c^2 \quad (3)$$

Using equations (2) and (3), p and c were estimated separately from the data on antibiotics derived from the two groups of organisms and for the pooled data. Using formula (1), the expected frequencies were computed. A χ^2 test was done. To fit the distribution, the upper tail of the distribution from duplication frequency 8 and above was omitted. Table 1 gives details of the goodness of fit. In all three cases, the goodness of fit was confirmed.

Table 1. OBSERVED AND EXPECTED FREQUENCIES OF DUPLICATIONS, 1907-19
TEST OF GOODNESS OF FIT

| No. of times duplicated | No. of antibiotics from fungi, algae and lichens | | No. of antibiotics from Actinomycetales | | Total | |
|-------------------------|--|-----------|---|-----------|----------------|----------|
| | Observed | Expected* | Observed | Expected† | Observed | Expected |
| 0 | 371 | 364.2 | 1,018 | 1,011.6 | 1,389 | 1,375.8 |
| 1 | 39 | 44.3 | 79 | 81.0 | 118 | 121.3 |
| 2 | 12 | 16.8 | 20 | 20.6 | 32 | 37.4 |
| 3 | 7 | 6.9 | 15 | 13.3 | 22 | 29.2 |
| 4 | 2† | 3.3 | 7 | 6.7 | 9 | 10.1 |
| 5 | 4† | 1.8 | 7† | 3.6 | 11 | 5.4 |
| 6 | 2† | 0.8 | 4† | 1.9 | 6† | 2.9 |
| 7 | 1† | 0.4 | 2† | 1.1 | 3† | 1.7 |
| χ^2_{df} | 0.28 | | 0.23 | | 1.25 | |
| | 0.49 for 4 df | | 12.49 for 4 df | | 12.99 for 4 df | |

* Value corrected to first decimal place.
† Grouped data used.

There thus seems to be predictable regularity in duplications, and Price's conjecture about the pattern of distribution of multiple discoveries is confirmed for antibiotics, even in cases where there are no duplications.

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Price, D. De B., *Little Science, Big Science*, 64 (Columbia University Press, New York, 1968).

Neelamohan, A., *Library Science with a Slant to Documentation*, 4, 51 (1968).

Kendall, M. G., and Stuart, A., *Advanced Theory of Statistics*, second ed., 1 (Hafner, New York, 1966).