# Segmentation Based on Measures of Contrast, Homogeneity, and Region Size

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Abstract — Two algorithms are described for automatic image segmentation using a "homogeneity" measure and "Contrast" measure defined on the cooccurrence matrix of the image. The measure of contrast involves the concept of logarithmic response (adaptibility with background intensity) of the human visual system. Provisions are also kept in two different ways to remove the undersithed thresholds. The effectiveness of the algorithms is demonstrated for a set of images having different types of histograms. The performance of the algorithms is compared to existing once.

#### L INTRODUCTION

One of the key problems in scene analysis is segmentation of a scene into different regions. Segmentation is essentially a pixel classification problem where one tries to classify the pixels into different classes such that each class is homograeous and at the same time the union of no two adjacent classes is homogeneous. In other words, given a definition of uniformity, segmentation is a partition of the picture into connected subsets, each of which is uniform but such that no union of adjacent subsets is uniform [1].

Several techniques of image segmentation exist, based on globa and local information of an image. One of the techniques based on global information is histogram thresholding which selects the valley points as threshold levels. For images where the histogram does not have sharp valleys (i.e., baving flan minima or local minima) the bistogram is usually sharpened [2]-[6] by a suitable transformation so that the task of selecting valleys becomes easier. These transformations usually require some parameters the choice of which has a significant impact in determining the number of thresholds. The cooccurrence marix, on the other hand, uses local spatial information of an image and provides information regarding the number of transitions between any two gray levels in the image. This information has been used by various authors, namely, Weszka and Rosenfeld [7], Deravi and Pal [8], and Chanda et al. [9], for segmentation.

The measures on the cooccurrence matrix reported by these authors did not consider the fact of logarithmic response of the homan visual system [10]-[13] in measuring "contrast" between regions in an image. The present work attempts to bring this factor into consideration while defining a measure of contrast in addition to defining another measure called bomogeneity within a region. The combination of these two measures made the algorithms effective in determining threshold levels. The contrast measure ensures three things. First, it assures the fact that transitions (change in the gray level) from  $i \ to \ i + l$  and a transition from  $i \ to \ i + k$ ,  $l \neq k$ , create different impressions. Second, a constant change in the gray level at different positions on the gray scale results in different impressions, and, finally, if the object and background intensities are interchanged, the contrast value remains unaltered.

Furthermore, provisions are also kept in two different ways for eliminating undesirable segments. In the first approach noninformative single gray level regions are eliminated by a separate

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merging algorithm. The second approach, on the other hand, inherently attempts to eliminate such smaller regions irrespective of their intensity width.

The effectiveness of the algorithms, along with a comparison with three other methods [7]-[9], has been demonstrated on a set of images. A Digital computer EC-1033 has been used for the analysis.

# II. COOCCURRENCE MATRIX AND SOME MEASURES FOR SEGMENTATION

#### A. Cooccurrence Matrix

Let  $F = \{f(x, y)\}$  be an image of size  $P \times Q$ , where f(x, y) is the gray value at (x, y) and  $f(x, y) \in G$ ,  $= (0, 1, 2, \cdots, L^{-})$ , the set of gray levels. The concourrence matrix (or the transition matrix) of the image F is an  $L \times L$  dimensional matrix that gives an idea about the transition of intensity between adjacent pixels. In other words, the (i, j)th entry of the matrix gives the number of times the gray level j (i)ows the gray level j (i.e., the gray level j i) an adjacent neighbor of the level j i) in a specific fashion

Let a denote the (i, j)th pixel in F and b denote one of the eight neighboring pixels of a, i.e.,

$$b \in a_{\kappa} = \{(i, j-1), (i, j+1), (i+1, j), (i-1, j), (i-1, j-1), (i-1, j-1),$$

$$(i-1,j+1),(i+1,j-1),(i+1,j+1)$$
.

Define

$$t_{lk} = \sum_{\substack{\alpha \in F \\ \delta \in A}} \delta$$

where  $\delta = 1$  if the gray level value of a is l and that of b is k;  $\delta = 0$ , otherwise.

Obviously,  $t_{II}$  gives the number of times the gray level k follows gray level l in any one of the eight directions. The matrix  $T = [t_{II}]_{k,I}$ , is, therefore, the cooccurrence matrix of the image F. One may get different definitions of the cooccurrence matrix by considering different subsets of  $a_1$ , i.e., considering  $b \in a_1^l$  where  $a_1^l \subset a_n$ .

The cooccurrence matrices may be either nonsymmetric or symmetric. One of the nonsymmetrical forms can be defined considering

$$t_{lk} = \sum_{l=1}^{p} \sum_{i=1}^{Q} \delta \tag{1}$$

with

$$\delta = 1$$
, if  $f(i, j) = l$  and  $f(i, j + 1) = k$   
or  $f(i, j) = l$  and  $f(i + 1, j) = k$ ;

On the other hand, the following definition of  $t_{ik}$  gives a symmetric cooccurrence matrix:

$$t_{jk} = \sum_{i=1}^{P} \sum_{j=1}^{Q} \delta$$

where

=1, if 
$$f(i,j) = l$$
 and  $f(i,j+1) = k$   
or
$$f(i,j) = l \text{ and } f(i,j-1) = k$$
or
$$f(i,j) = l \text{ and } f(i+1,j) = k$$
or
$$f(i,j) = l \text{ and } f(i-1,j) = k;$$



Pig. 1. Pictorial representation of busyness measure.

## B. Measures for Thresholding

Since the cooccurrence matrix contains information regarding the spatial distribution of gray levels in the image, several workers have used them for segmentation. For thresholding at gray level s, Weszkia and Rosenfeld [7] defined the busyness measure as follows:

busy(s) = 
$$\sum_{i=0}^{s} \sum_{j=s+1}^{L-1} t_{ij} + \sum_{i=s+1}^{L-1} \sum_{j=0}^{s} t_{ij}$$
. (3)

The cooccurrence matrix used in (3) is symmetric (using (2)).

The sum of the entries of the shaded portion in Fig. 1 represents the busyness measure for the level s. For an image with only two regions, say, object and background, the value of s for which the minimum of busy(s) occurs gives the threshold. Similarly, for an image having more than two regions, the busyness measure provides a set of minima corresponding to different thresholds.

Derayi and Pal [8] have given a measure for the conditional probability of transition from one region to another using a nonsymmetric cooccurrence matrix:

$$t_{ik} = \sum_{i=1}^{P} \sum_{i=1}^{Q} \delta \tag{4}$$

mit

$$\delta = 1$$
, if  $f(i, j) = l$ ,  $f(i, j+1) = k$ , and  $f(i+1, j) = k$ :  
 $\delta = 0$ , otherwise.

If the threshold is at s, the conditional probability of the intensity transition from the region [0, 1 to [s+1, -1], i.e., the probability of any intensity level from the class [0, 2] being followed by a level from the class [s+1, L-1] in the fashion given by (4), is

$$P_{1} = \frac{\sum_{i=0}^{r} \sum_{j=r+1}^{L-1} t_{ij}}{\sum_{i=0}^{r} \sum_{j=0}^{r} t_{ij} + \sum_{j=0}^{L-1} \sum_{j=0}^{L-1} t_{ij}}.$$
 (52)

Similarly, the conditional probability of the intensity transition from the region [s+1, L-1] to [0, s] is

$$P_{2} = \frac{\sum_{i=s+1}^{L-1} \sum_{j=0}^{s} t_{i,j}}{\sum_{i=s+1}^{L-1} \sum_{j=0}^{L-1} t_{i,j} + \sum_{i=s+1}^{L-1} \sum_{j=0}^{s} t_{i,j}}$$
(5b)

The conditional probability  $P_c(x)$  of transition across the boundary is defined as

$$P_{c}(s) = (P_{1} + P_{2})/2.$$
 (6)

The lower the value of  $P_i(t)$ , the lower is the probability of transition across the boundary between two classes [0,t] and [t+1,L-1]. That means, a minimum of  $P_i(t)$  will correspond to a threshold such that most of the transitions are within the class and few are across the boundary. Therefore, a set of minima of  $P_i(t)$  would be obtained corresponding to different thresholds in  $P_i(t)$  would be obtained corresponding to different thresholds

Chanda et al. [9] have also used the cooccurrence matrix for thresholding. They defined an average contrast (AVC) measure

$$AVC(s) = \frac{\sum_{i=0}^{r} \sum_{j=r+1}^{L-1} t_{i_j} * (i-j)^2}{\sum_{i=0}^{r} \sum_{j=r+1}^{L-1} t_{i_j}} + \frac{\sum_{i=r+1}^{L-1} \sum_{j=0}^{r} t_{i_j} * (i-j)^2}{\sum_{i=r+1}^{r} \sum_{j=0}^{r} t_{i_j}}$$
(7)

AVC(s) shows a set of maxima corresponding to the thresholds among various regions in F.

In the computation of t, they considered only vertical transitions in the downward direction. Note here that all of the three measures described before are basically based on some weighted combinations of the number of entries in the shaded and blank regions of Fig.

# III. SEGMENTATION BASED ON CONTRAST AND HOMOGENEITY MEASURES

In this section we present an algorithm for segmentation on the basis of the information of contrast and bomogeneity (between/within the regions in F) as obtained from the cooccurrence matrix (1). The concept of the human visual system has been microporated in the contrast measure to make the segmentation closer to the way a human being makes use of the intensity distribution for segmentation (of course, human beings use high level knowledge, too). Such a segmented image, when used for enhancement, will result in a better enhanced image as the method of segmentation ties to simulate the way a human being perceives the intensity variation. Before describing the algorithm, let us first explain some facts of the human visual system.

#### A. Human Psychovisual Facts

In psychophysiology contrast C refers to the ratio of difference in luminance of an object  $B_0$  and its immediate surrounding B [12], i.e.,

$$C = |B_0 - B|/B = \frac{\Delta B}{B}. \tag{8}$$

The perceived grayness of a surface depends on its local background and the perceived contrast remains constant if the measure C of the contrast between object and local background remains constant.

The visual increment threshold (or just noticeable difference) is defined as the amount of light  $\delta B_T$  necessary to add to a visual field of intensity B such that it can be discriminated from a reference field of same intensity B. It, therefore, gives a limit for a perceivable change in luminosace or intensity

At the low-intensity near absolute visual threshold (the mere presence or absorce of light intensity detectable under dark-adapted condition), the visual increment threshold  $\Delta B_z$  is constant. With increasing  $B_z \Delta B_z$  can be approximated by a linear function of  $B_z$  i.e.,  $\Delta B_y = a B$  (the factor a is called the Weber faitor. When this linear relationship is valid, one speaks of "Weber behavior."

Fig. 2 presents such a characteristic response in the  $\log \Delta B_T - \log B$  plane. The Weber behavior is characterized by unit slope of the curve. The preceding region with slope 1/2 is known as the De Vries-Rose region, characterized by  $\Delta B_T = \alpha_1 \sqrt{B}$ , which is a

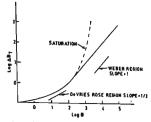


Fig. 2. Variation of  $\log \Delta B_y$  with  $\log B$  (in arbitrary scale) [10].

valid approximation only followed in a small restricted region. Under saturation, the visual increment threshold  $\Delta B_T$  does not follow the Weber behavior, and this deviation from Weber behavior is shown by the dashed line [10].

Therefore, if the brightness value of an object is higher (lower) than its surrounding or background or a reference intensity  $\vartheta$  by such an amount that it corresponds to a point on or above the curve (Fig. 2), the object will only then appear brighter (darker), i.e., discriminable to the human visual system (HVS). Furthermore, an equal amount of  $\Delta\vartheta$  value created at a different background intensity ( $\vartheta$  value) does not result in an equal perceivable change to the HVS. For example, the discrimination ability in the De Vries-Rose region is greater than in the Veber region, and this ability decreases with an increase in the value of  $\vartheta$ . The possible reason for this deterioration is discrimination ability can be attributed to nonlinearities inherent in the visual system.

## B. Measures of Contrast and Homogeneity

It has already been discussed that the problem of segmentation is to partition the set  $G_k$  of gray levels into some nonintersecting subsets such that each segment is as homogeneous as possible while the contrast between any segment and its neighboring segments is as high as possible. Two such measures, namely, the contrast of a segment with its neighboring segments and the homogeneity of a segment, are defined in the following. A composite measure of the two is then used to select the threshold levels in the immage F.

Let the gray levels ranging from K to M form one of the segments, say  $R_1$ , of the image F, i.e.,  $R_1 = [K, M], K \leqslant M$ . Define  $C_{K,M}^{B}$ , the contrast of the segment  $R_1$  with respect to other segments, as follows:

$$C_{R,M}^{g} = \frac{\sum_{i \in R_{i}} \sum_{j \in R_{i}} t_{i_{j}} * W_{i_{j}}}{C_{1} * \sum_{i \in R_{i}} \sum_{j \in R_{i}} t_{i_{j}}} = \frac{\sum_{i=1}^{M} \sum_{j \in R_{i}} t_{i_{j}} * W_{i_{j}}}{\sum_{j \in M} \sum_{j \in M} t_{i_{j}}} \cdot (9)$$

From Section III-A and Fig. 2 it is seen that because of the logarithmic behavior of the HVS the discrimination ability decreases with an increase in the value of background intensity B. This is what is also reflected by the contrast measure C defined in (8). To incorporate this property, we have introduced the weighting factor  $W_1$  in (9). However, note that the direct use of  $\Delta B/B$  for  $W_1$ , will

However, note that the direct use of  $\Delta B/B$  for  $W_{i,j}$  will obviously change the contrast value if the object and background intensities are interchanged. Since this is not intuitively appeal-

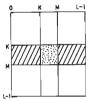


Fig. 3. Pictorial representation of contrast and homogeneity measures

ing, W,, may be defined as either

$$W_{ij} = |i - j|/(i + j), \qquad (10a)$$

$$W_{i,j} = |i - j|/\max\{i, j\},$$
 (10b)

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$$W_{i,j} = |i - j|/\min\{i, j\}.$$
 (10c)

It is, therefore, seen that  $W_{ij}$  ensures equal contribution to (9) when the object and background intensities are interchanged in addition to the property of deterioration of discrimination ability with increase in the background intensity.

In case of a complex image, the visual system does not adapt to a single intensity level; instead, it adapts to an average level which depends on the nature of the image [14]. It is, therefore, more logical to choose (10a) for  $W_f$ . In the denominator of (9) the term  $\Sigma \Gamma_f$ , is used to make the measure independent of the size of regions while the constant  $C_i$  is introduced to make  $0 < C_K^*$ , M < 1.  $C_i$  obviously depends on the choice of  $W_f$ , and is equal to the maximum possible value of  $W_f$ . Therefore,

$$C_1 = \begin{cases} (L-1)/(L+1), & \text{for (10a)} \\ (L-1)/L, & \text{for (10b)} \\ (L-1), & \text{for (10c)} \end{cases}$$

where L is the maximum level in F.

Therefore, it appears from (9) that if i = j, then  $C_{R,M}^2 = 0$ , i.e., the contrast in [K, M] is minimum. On the other hand, if i = 1 and j = L, then the contrast is maximum (=1) since for all  $i_j$  that are considered in  $C_{R,M}^2$  the values of  $W_j$  become equal to  $C_j$ , thereby making the numerator and denominator same.

The  $i_j x_j$  considered in (9) are shown by the shaded portion in

The  $t_{i,j}$  considered in (9) are shown by the shaded portion in Fig. 3, which gives the total number of transitions across the boundary of the segment  $R_1$ , i.e., from the region (K, M) to its

Again, define  $C_{K,M}^{W}$ , the homogeneity of the region [K,M], as

$$C_{K,M}^{W} = 1 - \frac{\sum\limits_{i = R_{1}} \sum\limits_{j = R_{1}} i_{ij} * |i - j|}{(L - 1) * \sum\limits_{j = R_{1}} \sum\limits_{j = R_{1}} i_{jj}} = 1 - \frac{\sum\limits_{i = K}^{M} \sum\limits_{j = K}^{M} i_{ij} * |i - j|}{(L - 1) * \sum\limits_{i = K}^{M} \sum\limits_{j = K}^{M} i_{ij}}$$
(11)

The  $t_{i,j}$  considered in (11) are shown by the dotted portion in Fig. 3.  $C_{i,j}^{\mu}$  lies in the interval [0,1], i.e.  $0 < C_{i,j}^{\mu} < 1$ . If  $R_1$  is perfectly homogenous, K = M (i.e., the region contains only one gray level), then  $C_{i,j}^{\mu} = 1$  as |l-j| = 0 for all l and J.

With the decrease of the homogeneity of  $R_i$ , [i-j] increases and approaches (L-1). As a result, the ratio in (11) approaches to unity and  $C_{K,M}^{\alpha}$  ends to zero. Thus  $C_{K,M}^{\alpha}$  and  $C_{K,M}^{\alpha}$  are found to increase with increase in contrast and homogeneity, respectively, in a region [K,M]. On the basis of these two

measures we define a composite measure:

$$g_{K,M}(C_{K,M}^{W}, C_{K,M}^{B}) = C_{K,M}^{W} \circ C_{K,M}^{B}. \tag{12}$$

Since  $0 < C_{N,M}^{H} < 1$  and  $0 < C_{N,M}^{H} < 1$ , g also lies between 0 and 1. The level at which g attains a maximum value can, therefore, be considered a boundary (or threshold) between regions.

## C. Extraction of Starting Regions - Algorithm 1

To extract the thresholds in an image F, we start with  $R_1 = [0,0]$  and increase the size of  $R_1$  one by one to the right side of the gray scale until we get a local maximum of  $R_{K,M}$ , i.e., the process is started with K = 0, M = 0, and M is incremented one by one until  $R_{K,M}$  attains a maximum value. If the maximum occurs at the gray level  $K_1$ , then  $K_1$  corresponds to a threshold and gray levels ranging from 0 to K, represent a region of the image F. Then we start with  $K = M = K_1 + 1$ , and the process is repeated as described until we get the next maximum, say at  $K_2$ . The gray levels ranging from  $K_1 + 1$  to  $K_2$  thus constitute another segment. In this way the process is carried on until the entire gray scale is exhausted.

Merging of Single-Valued Regions: The composite measure  $g_{K,M}$  is found to be very sensitive to highly uniform regions. In other words, a region containing only one gray level is likely to be detected as a separate segment, although one does not desire to have such a segment. To avoid this we have suggested here amerging algorithm whereby such a single-valued segment is accepted if the transitions within the segment are higher than those across it. This criterion enables one to retain only those regions which have significant size in the spatial domain.

Therefore, the algorithm first of all finds out the regions of single gray level and determines whether such regions should be merged or not. If it decides to merge a region, then the next task is to determine the adjacent region (left or right) to which it is to be merged.

Let  $R_i = [M, M]$  be the region under consideration. Let  $T_k$  be total number of transitions within the region  $R_i$ : then

$$T_{...} = t_{...}$$
 (13)

If  $T_0$  is the total number of transitions from R, to all other outside regions, then

$$T_0 = \sum_{i=M}^{M} \sum_{j,k,M} t_{ij}. \tag{14}$$

Decision Rule: If  $T_{w} > T_{0}$ , then the size of the region can be taken as reasonably big. Therefore, accept the region: do not merge it; otherwise, merge the region to either of its adjacent regions. Now the problem is to select the adjacent region to which it is to be merged.

Case 1: If M = 0, merge R, to the right adjacent region.

Care 2: If M = L - 1, merge R, to the left adjacent region Care 3: If 0 < M < L - 1, we proceed as follows. Left be the total number of transitions from R, to its left adjacent region. If the left adjacent region contains gray levels ranging from L, to  $L_1$ , then

$$T_L = \sum_{i=1}^{M} \sum_{j=1}^{L_2} \epsilon_{ij}. \tag{15}$$

Suppose  $T_R$  is the total number of transitions from R, to the right adjacent region and the right adjacent region contains gray levels ranging from  $R_1$  to  $R_2$ , then

$$T_R = \sum_{i=M}^{M} \sum_{j=R_i}^{R_2} t_{ij}$$
. (16)

If  $T_L > T_R$ , then merge  $R_i$  to the left adjacent region; otherwise merge it to the right adjacent region.

The foregoing decision rule can also be formulated in a more seneral way as follows. Let T, be the total number of transitions from R, to all regions including itself, i.e.,

$$T_i = \sum_{i=1}^{M} \sum_{j=0}^{L-1} i_{ij}$$
 (17)

and

$$\theta = T_w / T_s$$
,  $\theta < 1$ .

Now if  $\theta > \theta_H$ , accept the region, otherwise, merge it, where  $\theta_H$ is some preassigned threshold value.  $\theta_{ij} = 0.5$  obviously gives the original decision rule. The advantage of defining the decision rule in this manner is that in an interactive environment one can change \$\textit{\textit{\textit{\textit{\textit{\text{change}}}} \textit{\text{fit}}, if necessary, and compare the results to pick up the most appropriate value of  $\theta_H$  for a particular type of image.

## D. Incorporating Size of Region - Algorithm 2

In Algorithm I we have incorporated a separate merging phase to climinate the undesirable small (noninformative) regions. The following algorithm introduces the concept of size of regions into the composite measure  $g_{K,M}$  (12) and thereby attempts to eliminate the need of a separate merging phase.

$$g'_{K,M} = g_{K,M} \circ \left(\frac{A_R}{A}\right) \circ \left(\frac{1}{d_R}\right)^a \tag{18}$$

where

- $A_R$  size of the region [K, M], i.e., number of pixel intensities in F which are in the range [K, M].
- size of the image,  $= P \cdot O$ . parameter, with 0 < a < 1.
- length of the region [K, M] = M K + 1.

The first factor  $(A_R/A)$  gives more weight to the regions of greater size, resulting in an increase in the gi, w value. Thus if the histogram of an image has a sharp valley, the go, walue is very likely to decrease when M is set at the valley point. On the other hand, for a small region with a weak valley, such a decrease in g' value (for detecting the region) is less likely to occur. In such a situation, note that the following region (valley) becomes much less likely to be detected because of the cumulative increase of region size d, and hence A.

To circumvent this situation, a second factor (1/dg)" is introduced which compensates the foregoing effect by reducing the value of g' with an increase in  $d_R$ , a controls the rate of decrease in the g' value. As a increases, the number of regions is likely to increase. To extract the thresholds under this algorithm we proceed in exactly the same way as we have mentioned earlier for Algorithm 1, considering gr u for gr u.

## IV. IMPLEMENTATION AND RESULTS

The segmentation algorithms are described in the Appendix. The algorithms are implemented on a set of four different images [14] having dimension 64×64 with 32 gray levels. Figs. 4(a), 5(a), 6(a), and 7(a) represent the original input images, while Figs. 4(b), 5(b), 6(b), and 7(b) represent the corresponding gray-level histograms. These images are produced on a line printer by over printing different character combinations for different gray levels.

Fig. 4(a) represents an image of Mona Lisa. Note that the gray-level histogram (Fig. 4(b)) is almost unimodal (having some local minima). When the proposed Algorithm 1 (without merging) is applied to it, four thresholds, namely, 0, 1, 6, and 17 are produced. The corresponding segmented image is shown in Fig. 4g), where different segments are represented by different textures. When the merging algorithm is applied to it, the segment [1, 1] (Table 1) is merged to its right adjacent segment. The segmented image so obtained after merging is shown in Fig. 4(c).



(4)

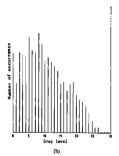


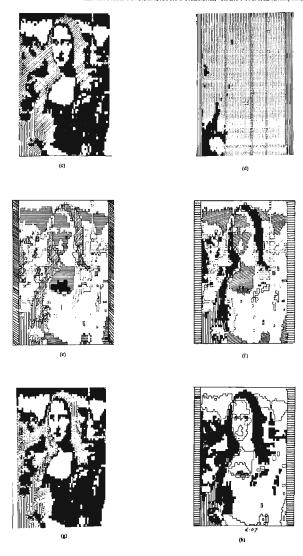
Fig. 4. (a) Input image of Mona Lisa. (b) Histogram. (c) Segmented image by proposed method 1. (d) Segmented image by [7]. (c) Segmented image by [8]. (1) Segmented image by [9]. (g) Segmented image by proposed method 1 (before merging). (h) Segmented image by proposed method 2.

Comparing Fig. 4(c) and Fig. 4(g), we find that an undesirable region exists inside the hair of Mona Lisa, which after being merged results in a more meaningful segmentation (Fig. 4(c)). Fig. 4(g) is shown, as an illustration, only to demonstrate the effect of the merging algorithm in selecting final thresholds.

Fig. 5(a) is an image of Abraham Lincoln, and the corresponding gray-level histogram (Fig. 5(b)) is found to have a number of deep valleys. The thresholds (before and after merging) generated by the proposed method I are shown in Table I. The output segmented image is shown in Fig. 5(c).

To demonstrate the validity of the method 1 for images with flat and wide valleys in their histogram, the algorithm is applied to the image of a jet (Fig. 6(a)). One can see in Fig. 6(a) that the right wing of the jet has vanished inside the cloud in such a way that apparently it is very difficult to trace the boundary of the right wing. Algorithm 1 is found to be successful in separating out that wing from the cloud. Fig. 6(c) represents the segmented image, while the thresholds are shown in Table I. As a typical illustration, Fig. 6(i) shows the plot of the gr. w value for the image of the jet.

Fig 7(a) represents the image of a biplane having two dominant modes in its histogram (Fig. 7(b)). From Fig. 7(c) the object is found to be clearly separated from the background.



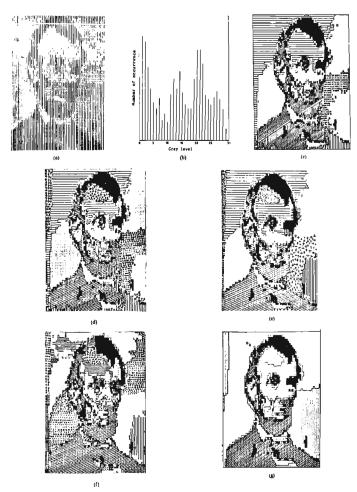


Fig. 5. (a) Input image of Lincoln. (b) Hastogram. (c) Segmented image by proposed method 1. (d) Segmented image by [7]. (e)
Segmented image by [8]. (f) Segmented image by [9]. (g) Segmented image by proposed method 2.

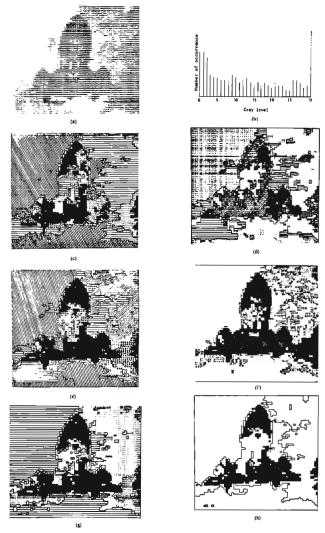


Fig. 6. (a) Input image of jet. (b) bissogram. (c) Segmented image by proposed method 1. (d) Segmented image by [7]. (c) Segmented image by 19, (f) Segmented image by proposed method 1 with β = 0.75, (h) Segmented image by proposed method 2 (i) Phot of E<sub>1</sub>, (ii) The of S<sub>2</sub>, (ii) for a = 0.5.

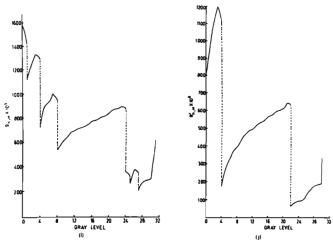


Fig. 6. Continued.

TABLE I Thresholds for Various Methods

	Proposed Method		Method of	Method of	Method of
image	Before	After	Wezska and	Deravi and	Chanda
	Merging	Merging	Rosenfeld [7]	Pal (8)	et al. [9]
Mona Lisa Fig. 4	0,1,6,17	0.6,17	0,30	0,3,6,17, 25,30	0, 3, 6, 17, 28, 30
Lincoln	0,4,9,13,17,	0,4,9,13,	0,4,9,12,17,	4,9,12,17,	5,10,12,17,
Fig. 5	18,24	17,24	24,30	23,30	22,27,30
Jei	0,3,7,23,	0,3,7,24,	0, 3, 5, 7, 18,	3,7,11,18	7,11,13,18
Fig. 6	24,26	26	29	29	21,23
Biplane	0,1,2,10	1,10,17	0.10.17.	0, 2, 10, 17,	0,10,14,17
Fig. 7	17,18,23	23	22,30	22, 30	21,29

TABLE 11
Thresholds for Different a

lmage	a = 0.2	a = 0.4	a = 0.6	a = 0.7	a = 0.8	a=1.0
Mona Lisa Fig. 4	17,28	6,25	0,6,25,28	0,6,17,24, 28	0,6,16,24, 25,28	0, 3, 6, 9, 14, 22, 24, 25, 28
Lincoln Fig. 5	5	4,17	4,9,17	4,9,17,29	4,9,17,24, 29	2,4,7,9,15. 17,23,29
Jet Fig. 6	7	3,23	3,21	3,21	3,7,16,23, 28	0,2,3,7,11, 13,16,19, 23,24,28
Biplane Fig. 7	10	10	8,10	1,10	0,7,10	2,7,9, 23,29

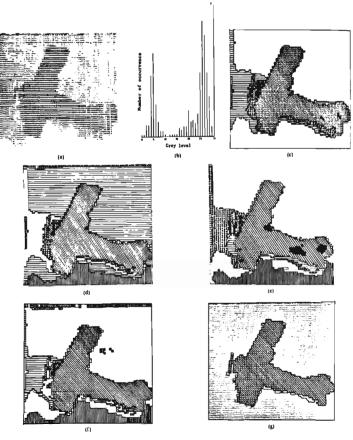


Fig. 7. (a) Input image of biplane. (b) Histogram. (c) Segmented image by proposed method 1. (d) Segmented image by [7]. (c) Segmented image by [8]. (f) Segmented image by [9]. (g) Segmented image by proposed method 2.

The aforementioned results were obtained by using (10a) while computing  $W_{j}$ , of the contrast measure. Experiments were also carried out with (10b), and the corresponding performances were found to be almost similar.

Table II shows the thresholds for these images obtained by the proposed Algorithm 2 for different values of a, As discussed in Section III-D, the number of segments is found to increase with increases in the value of a. Note, too, from Table II that the level 17 for Mona Lisa (unimodal histogram), which was detected at a = 0.2, was found to be missing for values of a = 0.4 and 0.6.

The threshold at 17 or its around again appeared for  $\alpha > 0.7$ . The case for jet is similar, having an almost flat and wide valleyed histogram where the level 7, which was detected at  $\alpha = 0.2$ , was lost at  $\alpha = 0.4$ , 0.6, and 0.7 and reappeared for higher  $\alpha$  values. Such a situation did not arise for the Lincoln and biplane images, which have deep valleys. This fact can be explained as follows:

Suppose the first threshold is detected at a gray level  $l = l_1$  for  $\alpha = \alpha_1$ , which means that g' kept on increasing up to gray kerd  $l_1$  and at  $(l_1 + 1)$ , g' started falling. Now if for a higher value of  $\alpha = \alpha_2$ ,  $\alpha_3 > \alpha_1$ , the first threshold is detected earlier at a gray

level  $l=l_2$ ,  $l_2 < l_1$ , then we can say that  $l_2$  is detected, as  $(1/d_R)^n$  has reduced the value of g' at  $(l_2 + 1)$  to a value which is less than the value of g' at I2. The threshold at I = I1, which was detected with  $a = a_1$ , may not now be detected with an a not much higher than a, because no sharp fall will occur in the g value as the histogram has weak valleys. Moreover, the value of  $(1/d_E)^*$  with  $d_B = l_1 + 1$  and  $\alpha = \alpha_1$  may be smaller than  $(1/d_B)^*$ with  $d_k = l_1 - l_2$ , and  $a = a_2$  as  $d_k$  in the second case is reduced to  $l_1$ . If from  $l_1 + l_2$  unless  $a_2$  is very high. Therefore, unless  $a_3$ is sufficiently high, the threshold at I, will not be detected. However, if the histogram has a deep valley at I, it will be detected because the fall in the g value will be sharp.

Figs 4(h), 5(g), 6(h), and 7(g) show the segmented images for Algorithm 2 when  $\alpha$  is considered to be 0.7, as an illustration. Fig. 6(1) shows the plot of the gr. w value for the image of the jet.

## Comparison with the Existing Algorithms

To compare the performance of the algorithms with those of some of the existing algorithms based on the cooccurrence mainx, we have considered algorithms of Weszka and Rosenfeld (3) [7]. Deravi and Pal (4)-(6) [8], and Chanda et al. (7) [9]. The thresholds obtained by these methods are also shown in Table I.

Equation (3) is found to fail to extract all the meaningful regions of the image of Mona Lisa. It has selected only three segments (Fig. 4(d)) with thresholds at 0 and 30; as a result, most of the important information is lost.

Equations (4)-(6), on the other hand, detected two extra segments in the chest and one extra region in the hair (Fig. 4(e)), while (7) also produced two similar segments (one of them is of smaller size than the corresponding one produced by (4)-(6) (Fig. 4(1)) From Fig. 4(c) it is seen that the regions generated by the proposed method 1, where these additional regions are absent, create a better impression to the eye. However, for Algorithm 2 (for n = 0.7) the hair of Mona Lisa did not split, and it has two extra regions in her chest (Fig. 4(h)).

For the image of Lincoln (Fig. 5) all the methods except the present ones have divided the forehead into two regions. Furthermore, Algorithm 1 and the method by Weszka and Rosenfeld have divided the beard into two regions, which is not the case for the other three methods. Finally, Algorithm 2 created the smallest number of segmented regions (Fig. 5(g)) and created a better imoression the eye.

In the case of the jet, (7) failed to discriminate between the cloud and the right wing (Fig. 6(f)) while the other two methods. like ours, are successful in doing so (Fig. 6(c)-(e)). Algorithm 1 and (3) produced comparable results, while the result produced by (4)-(6) (Fig. 6(e)) seems to create a better impression to the eye, but if we alter the value of  $\theta_H$  from 0.5 to 0.75 in the merging algorithm, the first two regions (Table I) are merged and the resulting image (Fig. 6(g)) is found to be much improved. However, Fig. 6(h) (by Algorithm 2), which has least number of segments, created the best result.

In the case of the biplane all the methods were able to detect its contour (Fig. 7). However, (4)-(6) are found to generate two additional regions inside the tail of the biplane which are absent for other cases. The background is found to be clustered in two paris by all but our methods. Furthermore, all the methods except ours divided the shade of the biplane into three or more regions, which is two and one for Algorithms 1 and 2, respec-

From Table I it appears that (3), (4)-(6), and (7) detected, except for the jet, a threshold at the end of the grey scale (e.g., 30 for Mona Lisa, Lincoln, and the biplane). These thresholds correspond to some undesirable regions at the frame of the images. The incorporation of the factor W,, in (9), which accounts for the nonlinear behavior of HVS, has been found to be able to eliminate such occurrences. However, Algorithm 2 failed to climinate such segments for higher value of a.

#### V. CONCLUSION AND DISCUSSION

Two algorithms for image segmentation are described using the measures of homogeneity and contrast within /between regions of an image. The first algorithm has a separate merging phase to climinate the undesirable segments. The second algorithm, on the other hand, eliminated the need of such a separate merging phase by considering the region size while extracting the thresholds. Both of the algorithms simulate the way in which human beings perceive brightness variation in an image.

Note here that when a human being attempts to segment an image, in addition to his logarithmic response to contrast he makes use of certain other higher level knowledge which is not considered in the proposed algorithms. Hence it is not expected that the proposed algorithms would segment an image exactly in the same way a human observer does. However, the incorporation of the weighting function W., to simulate only the contrast response of the human visual system has resulted in consistently better segments for images with different types of histograms

It is found that none of the existing methods could generate as consistently good segments as those of the proposed algorithms for all images. Some of the existing methods generated extra segments for some images, while some methods have failed to detect meaningful segments. Both of the proposed algorithms are suitable for an interactive environment.

It is seen that the choice of a in Algorithm 2 is critical. As a increases, the number of regions also increases, resulting in an acceptable segmentation around 0.5. However, for a good image baving sharp valleys in the gray level histogram, the typical value of a may be less than 0.5. On the other hand, an a greater than 0.5 can be taken for images having weak valleys in the histogram or a unimodal histogram.

The proposed methods are expected to be less sensitive to noise as the psychovisual facts have been considered. The work can be extended to three-dimensional images.

#### APPENDIX

Algorithm 1: Extraction of Initial Thresholds

Step 1 K = 0, M = 0, number of thresholds = 0. Step 2 Compute previous value = gh. M.

Step 3 M = M + 1

If M is greater than L-1, then go to step 6; otherwise, compute current value = gk, M

Step 4 Il current value is not less than previous value, then previous value = current value and go to Step 3

Number of thresholds = number of thresholds + 1. THRESHOLD (number of thresholds) = M - 1 (threshold is an array that stores the threshold levels), K = M, go to Step 2. Step 6 End of extraction of thresholds.

Merging Algorithm (Output of Algorithm 1 is Input to This Algorithm

Step 1 Find the next region of single gray level. If there is none,

then stop. Step 2 (Suppose the region under consideration is  $R = \{M, M\}$ ) Compute Tw = the number of transitions within R. Compute T. - the total number of transitions from R. to all other regions including itself. Compute  $\theta = T_{ii} / T_i$ 

Step 3 If  $\theta$  is greater than  $\theta_H$  (a predetermined value), then go to Step 1.

Step 4 If M is the first gray level with nonzero frequency, then merge the region R, to its right adjacent region and go to Step 1.

Step 5 If M is the last gray level with nonzero frequency, then merge the region R, to its left adjacent region and go to Step 1.

- Step 6 Compute T, and T, the number of transitions from R to its right and left adjacent regions, respectively.
- Step 7 If  $T_k$  is greater than  $T_k$ , then merge  $R_k$  to its left adjacent region. Otherwise, merge R, to its right adjacent region.
- Step 8 Go to Step 1.

# Algorithm 2

Replace  $g_{K,M}$  by  $g'_{K,M}$  in Algorithm 1. (Note that Algorithm 2 does not need the merging algorithm of Algorithm L.)

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